## The Paretian Optimum

## Efficiency in the Allocation of Factors among Commodities, or, Efficiency in Product-Mix or Composition of Output:

A composition of output or product-mix is Paretoefficient if it is impossible to increase the utility of one individual without reducing the utility of the other by reallocating the factors among the commodities, leading to a different product-mix.

The marginal condition for a Pareto-efficient product-mix states that the marginal rate of product transformation (MRPT) of  $Q_2$  into  $Q_1$  must be the same as the marginal rate of substitution (MRS) of  $Q_1$  for  $Q_2$ , for each consumer.

Here, the MRPT of  $Q_2$  into  $Q_1$  is equal to the quantity by which the production of  $Q_2$  has to be reduced in order to produce one more (or the marginal) unit of  $Q_1$  and, as such, it is equal to the numerical slope of the economy's production possibility curve or frontier (PPC or PPF). An economy's PPC passes through all the combinations of the two goods ( $Q_1$  and  $Q_2$ ) that the available quantities of the two inputs ( $X_1$  and  $X_2$ ) can produce Paretoefficiently. That is, any combination of the two goods that lie on the PPC gives us the maximum quantity of  $Q_1$  that can be produced subject to the production of a given

quantity of  $Q_2$ , or, the maximum of  $Q_2$  subject to a given quantity of  $Q_1$ .

In other words, the combinations of the two goods that lie on the PPC are those that lie on the Edge-worth contract curve for production (CCP) [Fig. 21.1]. That is, there is a one-to-one correspondence between the points on the CCP and those on the PPC. Since, as we move along the CCP, the quantity of one of the goods increases and that of the other decreases, the slope of the PPC would be negative.